

SELECTED SOLUTIONS

CHAPTER 6

Exercise Set 6.1.1

1. There is no error message. It simply draws the axes but not the point.
2. `plt.plot([-5,-4,-3,-2,-1,0,1,2,3,4,5],[5,4,3,2,1,0,1,2,3,4,5],'go')`
3. A. `xmin = 0, xmax = 4, xscl = .5, ymin = 50, ymax = 100, yscl = 1`
B. No it is not a function.
C. A more informative scaling would be `axis([0,5,0,100])`.
4. Scale the axes at $[-20,20] \times [-20,20]$ and draw the xy axes in black in the middle of the screen.

```
from matplotlib import pyplot as plt

plt.axis([-20,20,-20,20])
plt.plot([-20,20],[0,0], color='k')
plt.plot([0,0],[-20,20],color='k')
plt.show()
```

5. Write a program that will plot the following ordered pairs, connected with blue lines:

(1,1000), (2,750), (3, 1200), (4, 1450), (5, 1600), (6, 2000)

Label the x-axis as 'Month', the y-axis as 'Revenue', and the title of the graph 'Six Month Projection'.

```
from matplotlib import pyplot as plt

x_values = [1,2,3,4,5,6]
y_values = [1000,750,1200,1450,1600,2000]
plt.plot(x_values,y_values)          ## creates the plot object
plt.xlabel('Month')
plt.ylabel('Revenue')
plt.title('Six Month Projection')
plt.show()
```

Exercise Set 6.2.1

1. Slope between (4, 7) and (-2, 3) is $\frac{2}{3}$ (positive)

2. Slope between $\left(\frac{1}{3}, \frac{2}{5}\right)$ and $\left(\frac{5}{6}, \frac{1}{5}\right)$ is $-2/5$ (negative)
3. Slope between $(7, -8)$ and $(8, -8)$ is undefined (vertical)
4. Slope between $(2, 4)$ and $(3, -4)$ is -8 (negative)
5. $m_1 = 2$ and $m_2 = -2$ are neither
6. $m_1 = \frac{3}{9}$ and $m_2 = -3$ are perpendicular
7. $m_1 = 0$ and $m_2 = \text{undefined}$ are perpendicular

Exercise Set 6.2.2

1. The program does not work with fractions. Modify:

```
from fractions import Fraction
p1 = input('x1,y1? ')
x1,y1 = [Fraction(i) for i in p1.split(',')]
p2 = input('x2,y2? ')
x2,y2 = [Fraction(i) for i in p2.split(',')]
m1 = Fraction(y2-y1,x2-x1)
print('m=',m1)
```

2. No the program does not work when $x_1 = x_2$; you end up with an undefined slope. Modify:

```
from fractions import Fraction
p1 = input('x1,y1? ')
x1,y1 = [Fraction(i) for i in p1.split(',')]
p2 = input('x2,y2? ')
x2,y2 = [Fraction(i) for i in p2.split(',')]
if x1==x2:
    print('slope is undefined')
else:
    m1 = Fraction(y2-y1,x2-x1)
    print('m=',m1)
```

3. Write a program that asks the user to input the slopes of two lines, m_1 and m_2 . Compare the slopes. Output whether they are parallel, perpendicular, or neither. (*Hint: a pair of slopes m_1 and m_2 are opposite reciprocals if their product is -1 .*)

```
from fractions import Fraction
m1 = Fraction(input('m1? '))
m2 = Fraction(input('m2 '))
```

```

if m1==m2:
    print('parallel')
elif m1*m2==-1:
    print('perpendicular')
else:
    print('neither')

```

4. Write a program (or modify Program 6.2.1) that asks the user to input two ordered pairs (x_1, y_1) and (x_2, y_2) . Calculate the slope of the line through the two points, and also calculate and output the parallel and perpendicular slopes.

```

from fractions import Fraction
p1 = input('x1,y1? ')
x1,y1 = [Fraction(i) for i in p1.split(',')]
p2 = input('x2,y2? ')
x2,y2 = [Fraction(i) for i in p2.split(',')]
if x1==x2:
    print('slope is undefined')
    print('parallel slope is also undefined')
    print('perpendicular slope is zero')
elif y1==y2:
    print('slope is zero')
    print('parallel slope is also zero')
    print('perpendicular slope is undefined')
else:
    m1 = Fraction(y2-y1,x2-x1)
    print('m=',m1)
    print('parallel slope is m=',m1)
    m2 = -1/m1
    print('perpendicular slope is m=',m2)

```

Exercise Set 6.2.3

1. $y = (-5/2)x - 12$
2. $y = (5/8)x + 1/2$
3. $y = 8$
4. $x = 5/4$
5. $y = (2/3)x + 1/3$
6. $y = (3/7)x - 3$
7. $y = 5$

8. $y = -7x + 24$
9. $y = 8$
10. $x = 0$
11. $b = y - mx$
12. $y = -0.7x + 154$
13. Write a program to calculate target heart rate based on age.

```
x = int(input("Age? "))
print("Your target heart rate for moderate activity is")
print(-0.7*x + 154)
```

Exercise Set 6.2.4

1. $m = 4/5$, $b = -53/5$
2. Append the following statement to the program:

```
print(x1, y1, x2, y2)
```

3. When $x1 = x2$, it results in an undefined slope which is a vertical line. The error message can be circumvented with the following changes:

```
from matplotlib import pyplot as plt
from random import randint
from fractions import Fraction

x1 = randint(-10,10)
y1 = randint(-10,10)
x2 = randint(-10,10)
y2 = randint(-10,10)

plt.plot([x1,x2],[y1,y2])
if x1==x2:
    heading = 'x =' + str(x1)
else:
    m = Fraction(y2-y1,x2-x1)
    b = y1 - m*x1
    heading = 'y = (' + str(m) + ')x + ' + str(b)

plt.title(heading)
plt.show()
```

4. When $y1 = y2$, it results in a zero slope which is a horizontal line.

5. Modify the program so that the user can enter values for x1,y1 and x2,y2.

```
from matplotlib import pyplot as plt
from fractions import Fraction

p1 = input('x1,y1? ')
x1,y1 = [Fraction(i) for i in p1.split(',')]
p2 = input('x2,y2? ')
x2,y2 = [Fraction(i) for i in p2.split(',')]

plt.plot([x1,x2],[y1,y2])
m = Fraction(y2-y1,x2-x1)

b = y1 - m*x1
heading = 'y = ('+str(m)+'x + '+str(b))

plt.title(heading)
plt.show()
```

6. Replace

```
plt.plot([x1,x2],[y1,y2])
```

with:

```
colors = ['b', 'g', 'r', 'c', 'm', 'y', 'k', 'w']
rc = randint(0, 7)
plt.plot([x1,x2],[y1,y2],c=colors[rc])
```

Exercise Set 6.2.5

1. Modify the program to prompt the user to enter xmin, xmax.

```
from matplotlib import pyplot as plt
from sympy import Symbol, sympify

x = Symbol('x')
domain = input('xmin, xmax? ')
xmin, xmax = [int(k) for k in domain.split(',')]
x_list = range(xmin,xmax+1)
y_list = [] # initialize y_list
f_str = input('function? ')
f = sympify(f_str)

# For each a in x_list, find f(a) and assign to y_list
y_list = [f.subs({x:a}) for a in x_list]
```

```
plt.plot(x_list,y_list,'o')
plt.show()
```

2. Modify the program so that the title of the graph is " $f(x) = mx + b$ over $[xmin, xmax]$ " in which the $m, b, xmin$ and $xmax$ reflect the actual values that were input.

Append the following 2 lines:

```
title="f(x) = "+str(m)+"x "+str(b)+" over ["+str(xmin)+","+str(xmax)+"]"
plt.title(title)
```

3. If $3x-17$ is input, and a domain of $[-25, 25]$, what are the coordinates of the left and right endpoints?

$f(-25) = -92$ so the left endpoint is $(-25, -92)$.

$f(25) = 58$, so the right endpoint is $(25, 58)$.

4. Modify the program so that a line is drawn instead of discrete dots.

Change:

```
x_list = range(xmin,xmax+1)
to:
x_list = [xmin,xmax+1]
```

and change:

```
plt.plot(x_list,y_list,'o')
to:
plt.plot(x_list,y_list)
```

5. CHALLENGE: Modify the program so that the user is also prompted to input a point. Draw a line through that point, perpendicular to the given line.

Append the following lines to the program.

```
:
:
# parallel line
m,b=Poly(f).coeffs()
point=input('x,y? ')
x,y = [int(k) for k in point.split(',')]
b2 = y-m*x
y_list2 = []
y_list2 = [ m*a+b2 for a in x_list ]
plt.plot(x_list, y_list2)
parallel = '(' + str(m)+'*x'+str(b2)
title = 'Parallel Line is f(x)= ' + parallel
plt.title(title)
```

```
plt.show()
```

Exercise Set 6.2.6

1. What are the ymin and ymax of $f(x) = \frac{1}{10}(x^3 - 6x^2 - 27x + 140)$?
The minimum occurs at $f(-10) = -119$. The maximum occurs at $f(10) = 27$.

2. `plt.text(10, -10, 'Lisa')`

3. Output vertex if quadratic.

Append the following lines:

```
if degree(f)==2:
    a,b,c = Poly(f).all_coeffs()
    vx = -b/(2*a)
    vy = f.subs({x:vx})
    plt.plot([vx],[vy], 'o')
    ordered_pair = "(" + str(round(vx,0)) + "," + str(round(vy,0)) + ")"
    plt.text(vx,vy,ordered_pair)
```

4. Modify program **function_plot** to draw the x- and y-axes.

Append the following lines:

```
ymin = min(y_list)
ymax = max(y_list)
plt.plot([xmin,xmax],[0,0],c='k') # plot the x-axis
plt.plot([0,0],[ymin,ymax],c='k') # plot the y-axis
plt.plot(x_list,y_list)          # plot the function
```

5. Modify program **function_plot** to determine if a point is on the graph.

Append the following lines:

```
point = input('point? ')
a, b = [int(k) for k in point.split(',')]
plt.plot([a],[b], 'o')
p = '(' + str(a) + ',' + str(b) + ')'
plt.text(a,b,p)
if f.subs({x:a})==b:
    print(p,'is on the graph')
else:
    print(p,'is not on the graph')
plt.show()
```

Exercise Set 6.2.7

1.

Exercise Set 6.3.1

1. $3\sqrt{10}$

2. $5\sqrt{10}$

3. The lengths of the 3 sides are 72.1, 130, 108.2. Yes it is a right triangle because the slope from (0,0)-(60,40) is $\frac{2}{3}$ and the slope from (0,0) to (-60,90) is $-\frac{3}{2}$.

4. Write a function **distance**(x1,y1,x2,y2) that calculates and returns the distance between two points. Call the function from a main program. Output the answer as both a decimal and a simplified radical expression.

```
from sympy import *
import math

def distance(x1,y1,x2,y2):
    d = math.sqrt((x2-x1)**2+(y2-y1)**2)
    return d          # returns float value using math sqrt()

# main program
x = Symbol('x')
point1 = input('x1,y1? ')
x1,y1 = [int(i) for i in point1.split(',')]
point2 = input('x2,y2? ')
x2,y2 = [int(i) for i in point2.split(',')]

r = (x2-x1)**2 + (y2-y1)**2    # radicand
rad = sqrt(r)                 # simplified radical using SymPy sqrt()
pprint(rad)
print(distance(x1,y1,x2,y2))
```

5. Modify the main program you wrote in #4 so that it also graphs the line segment between the two points. Output the distance as a title, rounded to 1 decimal point.

```
from matplotlib import pyplot as plt
import math
```



```

def distance(x1,y1,x2,y2):
    d = math.sqrt((x2-x1)**2+(y2-y1)**2)
    return d

# main program
point1 = input("Point 1? ")
point2 = input("Point 2? ")

x1,y1 = [int(i) for i in point1.split(',') ]
x2,y2 = [int(i) for i in point2.split(',') ]

plt.plot([x1,x2],[y1,y2])

d = distance(x1,y1,x2,y2)
d = round(d,1)

plt.title("Distance is "+str(d))
plt.show()

```

6. 35.9

Exercise Set 6.3.2

1. A. $3\sqrt{22} \approx 14.07$

B. $\sqrt{690} \approx 26.27$

2. Modify program 3dplot so that it also prints the distance between the two points.

```

from sympy import *
from matplotlib import pyplot as plt

ax = plt.axes(projection="3d")      # declare ax as an alias for plt.axes
ax.plot3D([0,10],[0,10],[0,10])
ax.set_xlabel('x axis')
ax.set_ylabel('y axis')
ax.set_zlabel('z axis')
r = (10-0)**2 + (0-10)**2 + (10-0)**2
rad = sqrt(r)
title = 'Distance is '+str(rad)
plt.title(title)
plt.show()

```

3. Modify program 3dplot so that it allows the user to input any two ordered triples.

```

from matplotlib import pyplot as plt

```

```

from sympy import *

ax = plt.axes(projection="3d")      # declare ax as an alias for plt.axes
point1 = input("Point 1? ")
point2 = input("Point 2? ")

x1,y1,z1 = [int(i) for i in point1.split(',')]
x2,y2,z2 = [int(i) for i in point2.split(',')]

ax.plot3D([x1,x2],[y1,y2],[z1,z2])
ax.set_xlabel('x axis')
ax.set_ylabel('y axis')
ax.set_zlabel('z axis')
r = (x2-x1)**2 + (y2-y1)**2 + (z2-z1)**2
rad = sqrt(r)
title = 'Distance is '+str(rad)
plt.title(title)
plt.show()

```

4.

Exercise Set 6.4.1

1. A. $\left(-\frac{9}{2}, \frac{19}{2}\right)$
 B. $\left(\frac{49}{2}, -\frac{9}{2}\right)$
2. (17, -11)
3. $a = 3 \rightarrow AC = 10$
4. Write a program that calculates the midpoint of a line segment.

```

from fractions import Fraction
point1 = input("Point 1? ")
point2 = input("Point 2? ")

x1,y1 = [int(i) for i in point1.split(',')]
x2,y2 = [int(i) for i in point2.split(',')]

xm = Fraction(x1+x2,2)
ym = Fraction(y1+y2,2)
print(xm, ',', ym)

```

5. Write a program that calculates the midpoint of a line segment. Draw the line segment and label the distance at the coordinate of the midpoint.

```
from matplotlib import pyplot as plt
from math import sqrt

def distance(x1,y1,x2,y2):
    d = sqrt((x2-x1)**2+(y2-y1)**2)
    return d

def midpoint(x1,y1,x2,y2):
    xm = (x1+x2)/2
    ym = (y1+y2)/2
    return xm,ym

# main program
point1 = input("Point 1? ")
point2 = input("Point 2? ")

x1,y1 = [int(i) for i in point1.split(',') ]
x2,y2 = [int(i) for i in point2.split(',') ]
plt.plot([x1,x2],[y1,y2])

d = distance(x1,y1,x2,y2)
d = round(d,1)

xm,ym = midpoint(x1,y1,x2,y2)
plt.text(xm,ym,d)
plt.show()
```

6. Write a program that asks the user to input one endpoint (x1,y1) and the midpoint (m1,m2) then calculates and outputs the coordinates of the other endpoint (x2,y2).

```
from matplotlib import pyplot as plt

point1 = input("Point 1? ")
midpoint = input("Midpoint? ")

x1,y1 = [float(i) for i in point1.split(',') ]
xm,ym = [float(i) for i in midpoint.split(',') ]
x2 = 2*xm - x1
y2 = 2*ym - y1

plt.plot([x1,x2],[y1,y2])

plt.text(x1,y1,point1)
```

```

p2text = str(x2)+' '+str(y2)
plt.text(x2,y2,p2text)

plt.text(xm,ym,midpoint)
plt.show()

```

7. Write a program that draws a square, then connects the midpoints of the square.

```

from matplotlib import pyplot as plt

plt.axis([-15,15,-15,15])
plt.plot([-10,10,10,-10,-10],[10,10,-10,-10,10],c='k')
plt.plot([0,10,0,-10,0],[10,0,-10,0,10],c='r')
plt.show()

```

8. The effect is setting the aspect ratio of the x- and y- axes the same (so that the square looks more like a square and less like a rectangle).

9.

Exercise Set 6.4.2

1. midpoint: $(1/2, 3, 5/2)$; distance = $5\sqrt{2}$

2. midpoint: $(9/2, 1/2, 1/2)$; distance = $\sqrt{435}$

3. Modify program 3dplot so that it calculates and labels the midpoint of the line segment.

```

from matplotlib import pyplot as plt

ax = plt.axes(projection="3d")      # declare ax as an alias for plt.axes
point1 = input("Point 1? ")
point2 = input("Point 2? ")

x1,y1,z1 = [int(i) for i in point1.split(' ')]
x2,y2,z2 = [int(i) for i in point2.split(' ')]

ax.plot3D([x1,x2],[y1,y2],[z1,z2])
ax.set_xlabel('x axis')
ax.set_ylabel('y axis')
ax.set_zlabel('z axis')
xm, ym, zm = (x1+x2)/2, (y1+y2)/2, (z1+z2)/2
mp = '('+str(xm)+' '+str(ym)+' '+str(zm)+')'
ax.text(xm,ym,zm,mp)
plt.show()

```

Exercise Set 6.5.1

1. $x^2 + y^2 = 12$
2. $(x - 2)^2 + (y + 3)^2 = 16$
3. Center: (2, -7); Radius: 6
4. $x^2 + y^2 + 10x + 4y - 20 = 0$
5. Center: (0, 2); Radius: $\sqrt{13}$
6. $(x - 3)^2 + (y + 2)^2 = 25$
7. $(x - 2)^2 + (y - 2)^2 = 5$
8. $(x - 2)^2 + (y - 3)^2 = 4$
9. Write a program that asks the user to input the center and radius of a circle. Output the equation of the circle in standard form.

```
center = input("center? ")
h, k = [int(i) for i in center.split(',')]
r = int(input("radius? "))
circle = '(x-' + str(h) + ')**2 + (y-' + str(k) + ')**2 = ' + str(r)
print(circle)
```

10. Write a program that asks the user to input the endpoints of the diameter (as in #7 above); output the equation of the circle in standard form.

```
from math import sqrt

point1 = input("Point 1? ")
point2 = input("Point 2? ")

x1,y1 = [int(i) for i in point1.split(',')]
x2,y2 = [int(i) for i in point2.split(',')]

d = sqrt((x2 - x1)**2 + (y2 - y1)**2)
r = d/2

h = (x1+x2)/2
k = (y1+y2)/2
r_squared = round(r**2,1)

print('(x-',h,')^2 + (y-',k,')^2 =',r_squared)
```

11. Write a program that asks user to input general form of a circle. Find the x-intercepts.

```
from sympy import *
x = Symbol('x')
circ = input('General form A,B,C,D,E: ')
A,B,C,D,E = [n for n in circ.split(',')]
gen = A+'x**2'+C+'x'+D+E
gen = sympify(gen)
zeros= solve(gen)
real = True;
for n in zeros:
    if n.is_complex:
        real = False;
if real == True:
    print(zeros)
else:
    print('no x-intercepts')
```

Exercise Set 6.5.2

1. A. $y = \pm\sqrt{81 - (x + 7)^2}$

B. $y = \pm\sqrt{9 - (x - 5)^2} - 1$

2. Fill in yellow highlighted code to draw lower semi-circle.

```
y_list2 = [-sqrt(r**2-(x-h)**2)+k for x in x_list]
plt.plot(x_list,y_list2)
```

Exercise Set 6.5.3

1. Write a program that draws a circle inscribed inside a square.

2. Write a program that draws a square inside a circle.

3. Write a program that generates and draws randomly placed circles in different colors on the screen.

```
from matplotlib import pyplot as plt
from random import randint
color = ['b','g','r','c','m','y']
for i in range(1,20):
    h = randint(1,10)
```

```

k = randint(1,10)
r = randint(1,10)
c = randint(0, 5)
circle=plt.Circle((h,k), r,ec=color[c],fc='white')
ax = plt.gca()
ax.add_patch(circle)
plt.axis('scaled')
plt.show()

```

4.

Exercise Set 6.6.1

1. A. The 3 vertices are at $(0, \frac{\sqrt{3}}{2} \cdot 7)$, $(-7/2, 0)$ and $(7/2, 0)$.
 B. The area is $\frac{\sqrt{3}}{2} \cdot 49$.
2. A. The 3 vertices are at $(0,10)$, $(-\frac{7}{2}, 10 - \frac{\sqrt{3}}{2} \cdot 10)$ and $(\frac{7}{2}, 10 - \frac{\sqrt{3}}{2} \cdot 10)$
 B. The area is $\frac{\sqrt{3}}{2} \cdot 49$.
3. The 3 vertices are at $(6, 9)$, $(4, 9 - \frac{\sqrt{3}}{2} \cdot 9)$ and $(8, 9 - \frac{\sqrt{3}}{2} \cdot 9)$

Exercise Set 6.6.2

1. Fill in the yellow highlighted code with:

```
plt.plot([0,x1,x2,0],[y,0,0,y])
```

2. Append the following two lines:

```

area = round((d**2)*sqrt(3)/2,2)
plt.annotate(area,xy=(0, y/2))

```

3. Modify program so that y-coordinate of vertex is at (0, f).

```

from matplotlib import pyplot as plt
from math import sqrt

d = float(input("Side length? "))
f = float(input("y-coordinate of top vertex? "))

# top vertex is (0,f)

```

```

# y-coordinate of base
y = f - d*sqrt(3)/2

# base vertices are at (x1, y) and (x2, y)
x1 = -d/2
x2 = d/2

plt.plot([0,x1,x2,0],[f, y, y, f])

area = round((d**2)*sqrt(3)/2,2)
# print area at midpoint
plt.annotate(area,xy=(0, (y+f)/2))
plt.show()

```

4. Modify the program so that the top vertex can be at any ordered pair (e, f).

```

from matplotlib import pyplot as plt
from math import sqrt

d = float(input("Side length? "))
vertex = input("Coordinates of top vertex? ")
e,f = [float(i) for i in vertex.split(',')]

# top vertex is (e,f)
# y-coordinate of base
y = f - d*sqrt(3)/2

# base vertices are at (x1, y) and (x2, y)
x1 = e-d/2
x2 = e+d/2

plt.plot([e,x1,x2,e],[f, y, y, f])

area = round((d**2)*sqrt(3)/2,2)
plt.annotate(area,xy=(e, (y+f)/2))
plt.show()

```

Chapter Project X: Linear System

```

from matplotlib import pyplot as plt
from sympy import *

def draw_axes(x_list,y_list):

```



```

x_min = min(x_list)
x_max = max(x_list)
y_min = min(y_list)
y_max = max(y_list)
plt.plot([x_min,x_max],[0,0],c='k')
plt.plot([0,0],[y_min,y_max],c='k')
return

# main program
x_list = range(-10,11)

x = Symbol('x')
func1 = sympify(input("Line 1? "))
func2 = sympify(input("Line 2? "))

y1_list = []
y2_list = []

for a in x_list:
    y1 = func1.subs{x:a}    # calculate y1(a)
    y1_list.append(y1)
    y2 = func2.subs{x:a}    # calculate y2(a)
    y2_list.append(y2)

plt.plot(x_list,y1_list)
plt.plot(x_list,y2_list)
draw_axes(x_list,y1_list)

m1,b1 = poly(func1).all_coeffs()
m2,b2 = poly(func2).all_coeffs()

if m1==m2:
    plt.title('Inconsistent')
    if b1==b2:
        plt.title('Consistent Dependent')
else:
    if m1*m2==-1:
        plt.title('Consistent Independent - Perpendicular')
    else:
        plt.title('Consistent Independent')
    equ = str(func1)+'-('+'str(func2)+'')
    s = solve(equ) # returns a list of solutions of func1 = func2
    a = s[0]

```

```
b = func1.subs({x:a})
op = '('+str(a)+'/'+str(b)+')'
plt.text(a,b,op)
```

Chapter Project XI: Nonlinear System

```
from matplotlib import pyplot as plt
from sympy import *
```

```
def draw_axes(x_list,y1_list,y2_list):
    x_min = min(x_list)
    x_max = max(x_list)
    y_min = min(y1_list+y2_list)
    y_max = max(y1_list+y2_list)
    plt.plot([x_min,x_max],[0,0],c='k')
    plt.plot([0,0],[y_min,y_max],c='k')
    return
```

```
# main program
```

```
x_list = range(-10,11)
```

```
x = Symbol('x')
```

```
func1 = sympify(input("Function 1? "))
```

```
func2 = sympify(input("Function 2? "))
```

```
y1_list = []
```

```
domain1 = []
```

```
for a in x_list:
```

```
    y1 = func1.subs({x:a})
```

```
    if (not y1.is_imaginary):
```

```
        domain1.append(a)
```

```
        y1_list.append(y1)
```

```
plt.plot(domain1,y1_list)
```

```
y2_list = []
```

```
domain2 = []
```

```
for a in x_list:
```

```
    y2 = func2.subs({x:a})
```

```
    if (not y2.is_imaginary):
```

```
        domain2.append(a)
```

```
        y2_list.append(y2)
```

```
plt.plot(domain2,y2_list)
```

```
draw_axes(x_list,y1_list,y2_list)
```

```
equ = str(func1)+'-('+'str(func2)+')
```

```
s = solve(equ) # returns a list of solutions of func1 = func2
```

```
for a in s:
```

```
    if (not a.is_imaginary):
```

```
        b = func1.subs({x:a})
```

```
        if (not b.is_imaginary):
```

```
            a = round(float(a),2)
```

```
            b = round(float(b),2)
```

```
            op = '('+'str(a)+'+'str(b)+'')
```

```
            plt.text(a,b,op)
```